

*Transport through a state with
negative binding energy in a
two-dimensional quantum wire*

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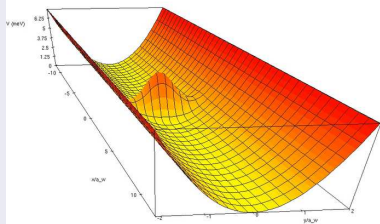
NCTS, June, 2005

Outline

- 1 System and model of Transport
- 1 Known results for an attractive scattering potential
- 1 Two bound 2D electrons
 - In the literature
 - Extending the idea
 - Conditions for a simple state
- 1 Transport in wire with a repulsive scatterer
 - Conductance
 - Perturbative view, virtual transitions
 - Bound states with negative binding energy
- 1 Related results of others
- 1 Conclusions

Model

Quantum wire

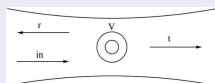


Scattering potential

- Narrow Gaussian shape
- Broad wire
 - Attractive
 - Repulsive

Model \leftrightarrow Transport

Quantum wire



- Single electron
- Multiple scattering
- General potential
- Analytic - numerical

T-matrix \leftarrow Lippmann-Schwinger

$$\tilde{T}_{nn'}(q, p) = \tilde{V}_{nn'}(q, p) + \sum_{m'} \int \frac{dk a_w}{2\pi} \tilde{V}_{nm'}(q, k) G_E^{m'}(k) \tilde{T}_{nm'}(k, p).$$

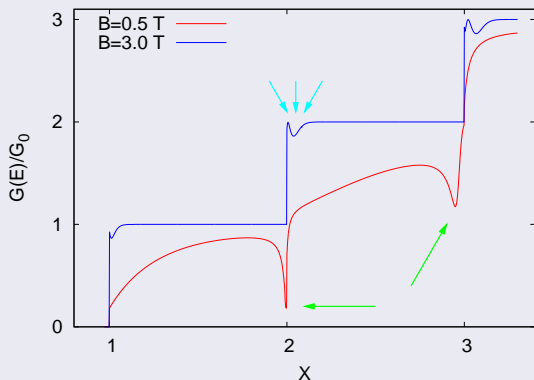
$$t_{nm}(E) = \delta_{nm} - \frac{i\sqrt{(k_m/k_n)}}{2(k_m a_w)} \left(\frac{\hbar\Omega_0}{\hbar\Omega_w} \right)^2 \tilde{T}_{nm}(k_n, k_m).$$

$$G(E) = \frac{2e^2}{h} \text{Tr}[\mathbf{t}^\dagger(E)\mathbf{t}(E)],$$

- Phys. Rev. B71, 235302 (2005)

Results

Conductance, attractive potential



$$G_0 = \frac{2e^2}{h}$$

$$X = \frac{E}{\hbar\Omega_w} + \frac{1}{2}$$

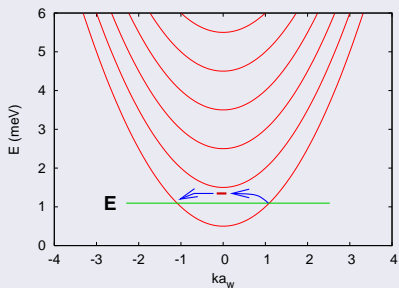
$$\Omega_w = \sqrt{\omega_c^2 + \Omega_0^2}$$

$$\hbar\omega_0 = 1.0 \text{ meV}$$

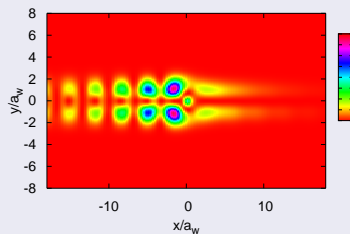
$$V_0 = -8.0 \text{ meV}$$

Evanescent States, $B = 0.5$ T, $V_0 = -8$ meV

Energy spectrum

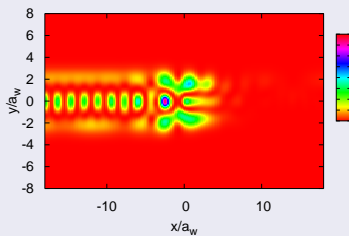


Instate: $n = 1$, $X = 1.9962$

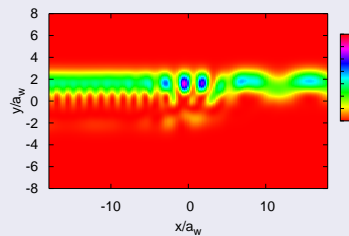


Evanescent States, $B = 0.5$ T, $V_0 = -8$ meV

Instate: $n = 2$, $X = 2.9482$

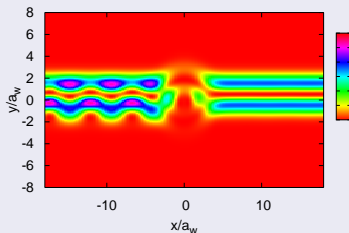


Instate: $n = 1$, $X = 2.9482$

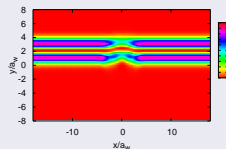
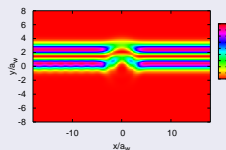


$$B = 3.0 \text{ T}, V_0 = -8 \text{ meV}$$

Instate: $n = 2$, $X = 2.0062$



Instate: $n = 2$, $X = 2.0382$, and
 $X = 2.0841$



“Quantized motion of three two-dimensional electrons in a Strong magnetic Field”,

R. B. Laughlin, Phys. Rev. B27, 3383 (1983)

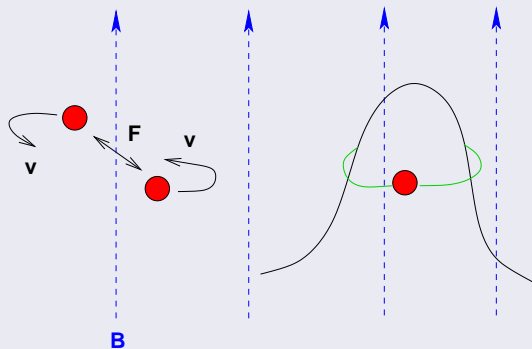
True in 2D:

*“The physical origin of the quantization of electron separation in our picture is that particles of like sign in a strong magnetic field **do not repel one another**, but orbit about their center of mass with a speed proportional to the Coulombic force between them.”*

*“Thus we have a physical picture in which the particles orbit one another at distance r , as they would in the absence of a Coulomb interaction, but with a **negative binding energy e^2/r** .”*

Idea

If true for two $e^- \rightarrow$ also true for one $e^- +$ hill



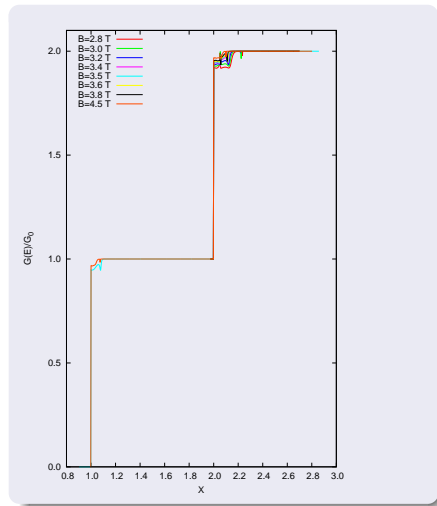
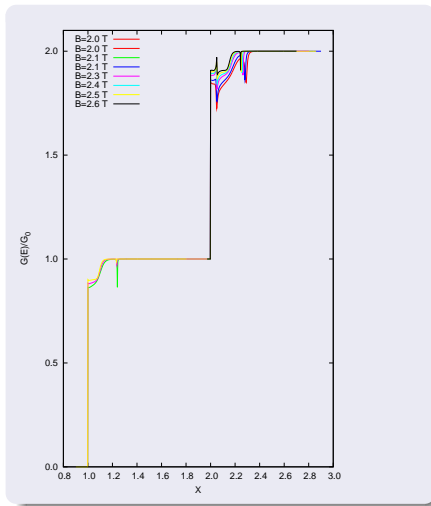
Can such a bound state be seen in transport?

\leftrightarrow Quasi-bound state in the *wire*

Conditions for a state with simple structure

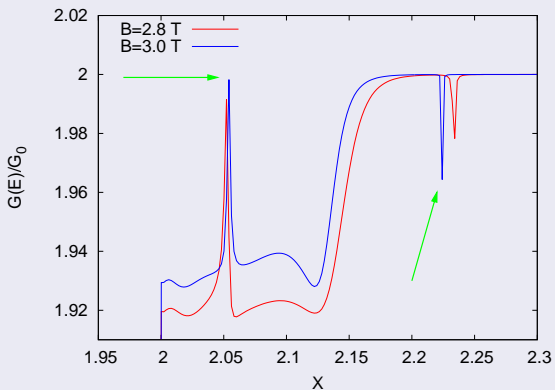
- Magnetic length \sim potential size \ll wire width
- Smooth (Gaussian) potential
- $V_0 \geq$ subband separation
- High E-resolution in calculation

Conductance, $V_0 = 8$ meV



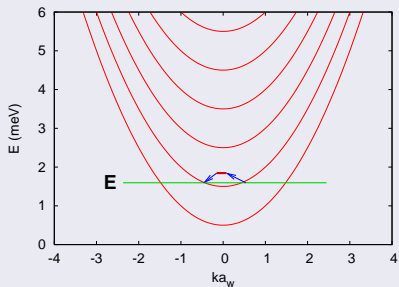
Conductance, $V_0 = 8$ meV

Magnification

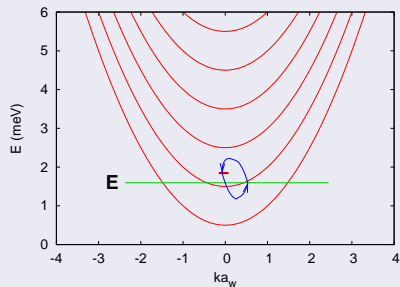


Energy spectrum, $V_0 = 8.0$ meV

Backscattering resonance



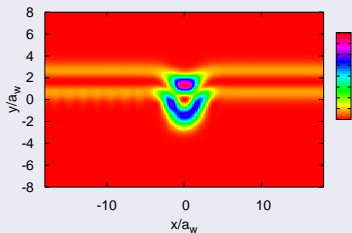
Forward scattering resonance



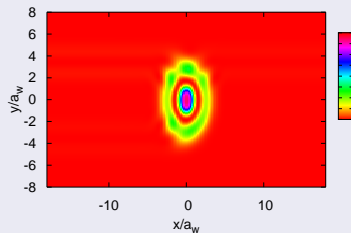
Probability density

Boundstate around a hill, narrow resonances

$n = 2, X = 2.0542, B = 3 \text{ T}$



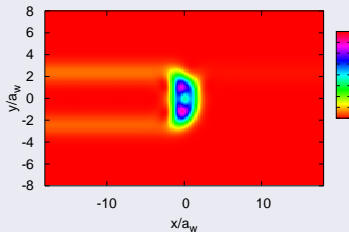
$n = 2, X = 2.242, B = 3 \text{ T}$



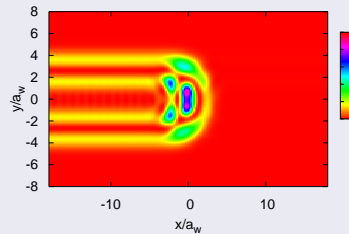
Probability density

Boundstate around a hill, $B = 2$ T

$n = 1$, $X = 1.2422$
lower energy

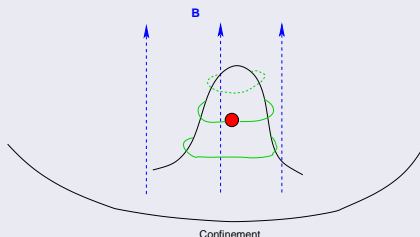


$n = 2$, $X = 2.29$
broad resonance



Structure of states

Quasi-bound states



Structure

- Upper states have simpler structure
- Edge influence on lower states
- Estimate by Bohr quantization
- Upper states difficult to see

Related results of others

- J. K. Jain and S. A. Kivelson, Phys. Rev. Lett. 60, 1542 (1988),
Smooth scatterer, QHE - narrow constrictions, Extreme Q-limit, one subband
- Y. Takagaki and D. K. Ferry, Phys. Rev. B 48, 8152 (1993),
Hard-wall large scatterer, tight-binding, AB-oscillations
- S. Chaudhuri, S. Bandyopadhyay and M. Cahay, Phys. Rev. B 47, 12649 (1993),
 δ -scatterer, QHE, magnetically bound state, vortex state

Conclusions

- Bound state with negative binding energy seen in transport calculation
 - Why difficult to notice in transport calculations
 - Smooth potential
 - Resolution
 - Overlap of wavefunctions, matrix elements
 - Several thousand CPU-hours
- Can it be seen in experiments?
- <http://arxiv.org/abs/cond-mat/0506009>
- See also:
 - Phys. Rev. B71, 235302 (2005),
 - Phys. Rev. B70 245308,(2004),
 - cond-mat/0411378