

Dæmi 1, (11-11-60)

$$\vec{B} = (B_x, 0, B_z) = (0,5, 0, 0,8) T$$

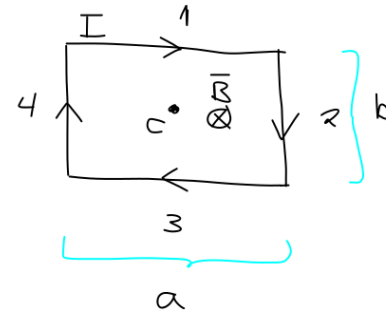
$$\vec{v} = (v_x, v_y, 0) = (3,0, 4,0) \cdot 10^6 \text{ m/s}$$

finna $\vec{F} = q \vec{v} \times \vec{B}$

$$\vec{F} = q \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ v_x & v_y & 0 \\ B_x & 0 & B_z \end{vmatrix} = q (v_y B_z, -v_x B_z, -B_x v_y)$$

①

Dæmi 2, (11-12-20)



Finna segulsvið í punktinum C í miðri lykkjunni \vec{B}_C

Hægrihandarreglan gefur okkur að segulsvið í C er inn í síðuna og

$$\vec{B}_4 = \vec{B}_2, \vec{B}_1 = \vec{B}_3$$

Ég nota jöfnur (12.5-6) með nauðsynlegri aðlögun

$$B_3 = \frac{\mu_0 I}{2\pi} \int_0^{a/2} \frac{R dx}{(x^2 + R^2)^{3/2}}, \quad R = \frac{b}{2}$$

notandi

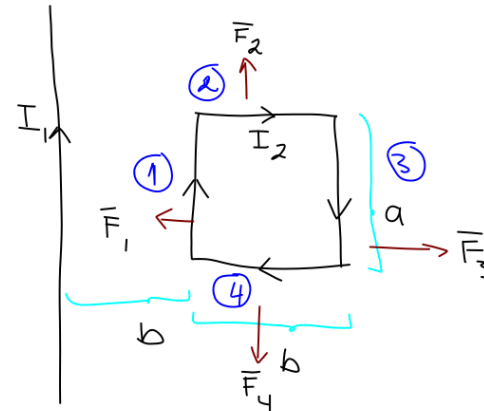
$$\int \frac{dx}{(x^2 + R^2)^{3/2}} = \frac{x}{R^2(x^2 + R^2)^{1/2}} + C$$

③

Dæmi 3, (11-12-34)

Finna heildarkraftinn á lykkjuna

$$d\vec{F} = I d\vec{l} \times \vec{B}$$



$$\vec{F}_2 + \vec{F}_4 = 0$$

$$\vec{F}_1 + \vec{F}_3 \neq 0$$

Á leiðurum 1 og 3 er segulsvið vegna 1, fast

$$B_3 = \frac{\mu_0 I R}{2\pi} \frac{a \sqrt{4R^2 + a^2}}{4R^4 + a^2 R^2} = \frac{\mu_0 I}{\pi b} \frac{1}{\sqrt{1 + (\frac{b}{a})^2}}$$

og á svipáðan hátt

$$B_4 = \frac{\mu_0 I}{\pi a} \frac{1}{\sqrt{1 + (\frac{a}{b})^2}}$$

$$\rightarrow B_{\text{Total}} = \frac{2\mu_0 I}{\pi b} \frac{1}{\sqrt{1 + (\frac{b}{a})^2}} + \frac{2\mu_0 I}{\pi a} \frac{1}{\sqrt{1 + (\frac{a}{b})^2}}$$

$$= \frac{2\mu_0 I}{\pi ab} \sqrt{a^2 + b^2}$$

②

④

$$F_1 = I_2 a \frac{\mu_0 I_1}{2\pi b}$$

$$F_3 = I_2 a \frac{\mu_0 I_1}{2\pi 2b}$$

$$\rightarrow F_1 > F_3$$

$$F_1 - F_3 = \frac{\mu_0 I_1 I_2 a}{2\pi} \left(\frac{1}{b} - \frac{1}{2b} \right)$$

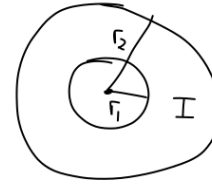
$$= \frac{\mu_0 I_1 I_2}{4\pi} \left(\frac{a}{b} \right)$$

$$\rightarrow \vec{F}_{\text{total}} = - \frac{\mu_0 I_1 I_2}{4\pi} \left(\frac{a}{b} \right) \hat{i} \quad \begin{array}{l} \text{með stefnu} \\ \text{að beina vörnum} \\ \text{með } I_1 \end{array}$$

5

Daemi 4, (11-12-46)

6



$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I$$

$$\text{Fyrir } r < r_1 \quad I_{\text{enc}} = 0 \rightarrow \vec{B} = 0$$

Fyrir $r > r_2$

$$2\pi r B = \mu_0 I$$

$$\vec{B}(r) = \frac{\mu_0 I}{2\pi r} \hat{\theta}$$

7

Fyrir $r_1 < r < r_2$

$$I_{\text{enc}} = I \left(\frac{r^2 - r_1^2}{r_2^2 - r_1^2} \right)$$

$$\rightarrow 2\pi r B = \mu_0 I \left(\frac{r^2 - r_1^2}{r_2^2 - r_1^2} \right)$$

$$\rightarrow \vec{B}(r) = \frac{\mu_0 I}{2\pi r} \left(\frac{r^2 - r_1^2}{r_2^2 - r_1^2} \right) \hat{\theta}$$